## $\Phi_{i} \quad$ segment fraction of component $i$ <br> Registry No. Ethanol, 64-17-5; acetonitrile, 75-05-8; chloroform, 67-66-3.

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# Excess Volumes for 2-Methyl-2-propanol + Water at 5 K Intervals from 303.15 to 323.15 K 

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#### Abstract

Excess volumes of mixtures of 2-methyl-2-propanol $\left(x_{\mathrm{a}}\right)+$ water ( $x_{w}$ ) have been measured at 5 K Intervals from 303.15 to 323.15 K by using a dilution dillatometer. The partial molar excess volume of 2-methyl-2-propanol at Infinite dilution In water Is extremely temperature-dependent, becoming more negative as the temperature increases. The partial molar excess volume of 2-methyl-2-propanol in dllute solutions with water ls very concentration-dependent and the dependence reduces as temperature increases. At $x_{\mathrm{a}}=0.019$, the partial excess volume of 2-methyl-2-propanol is Independent of temperature, having a value of $\mathbf{- 9 . 8 3} \mathrm{cm}^{3}$ $\mathrm{mol}^{-1}$, while the excess volume is independent of temperature at $x_{\mathrm{a}}=0.039$, having a value of -0.0376 $\mathrm{cm}^{3} \mathrm{~mol}^{-1}$ over the temperature range measured. These unusual observations are explained in terms of the varlation of the temperature of maximum density and hydrophoblc interaction for dllute 2-methyl-2-propanol solutions.


## Introduction

Volumetric properties of mixtures of alcohols with water have been investigated by numerous researchers. The nonideal behavior of these mixtures has been discussed on the basis of MacMillan-Mayer theory (1), scaled-particle theory (2), and the cosphere-solvation concept of Gurney (3, 4).

2-Methyl-2-propanol is of particular interest since it is completely miscible in water, although other $\mathrm{C}_{4}$ alcohol isomers are only partially miscible. Kenttamaa and co-workers (5) measured the densities of 2-methyl-2-propanol + water with an Oswald pycnometer from 288.15 to 323.15 K and reported the partial molar volumes covering the majority of the mole fraction range. Density measurements of 2-methyl-2-propanol + water were made by Nakanishi et al. (6) at 298.15 K with an accuracy of $\pm 1 \times 10^{-5} \mathrm{~g} \mathrm{~cm}^{-3}$ and the excess volumes were calculated over the whole composition range.

Frank and Smith (7) used a float technique to measure the densities of solution up to the molal concentration of $0.1\left(x_{\mathrm{a}}=\right.$ 0.018 ) at $273.65,278.15,298.15$, and 313.15 K with a precision of $\pm 1 \times 10^{-6} \mathrm{~g} \mathrm{~cm}^{-3}$. They discussed various methods of extrapolating density results to obtain the partial molar volume at infinite dilution, $V_{\mathrm{a}}{ }^{\infty}$, and suggested that, as $x_{\mathrm{a}}$ approaches zero, ( $\partial V_{\mathrm{a}} / \partial x_{\mathrm{a}}$ ) should approach zero rather than
have the temperature-dependent finite slope usually observed. Hvidt et al. (8) measured the densities of 2-methyl-2-propanol + water up to $x_{\mathrm{a}}=0.4$ between 278.15 and 298.15 K with an accuracy of $\pm 1 \times 10^{-5} \mathrm{~g} \mathrm{~cm}^{-3}$. They argued that the unusual apparent molar volumes at infinite dilution of alcohol were determined not only by an overlapping of hydrophobic cospheres but also by a shift in mobile equilibria between different structures in the water near the nonpolar groups. Jolicoeur et al. (9) measured densities of alcohol isomers using a flow densimeter and discussed the effect of alcohols on the structure of water. The variation of nonpolar group size and geometry of alcohols was not conclusively attributed to specific effects in the hydration of the alkyl groups.
Precise measurements of excess volumes over the whole composition range are necessary to understand the nature of interactions between nonpolar groups and water, the so-calied hydrophobic solvation. However, there have been no direct measurements of the excess volumes of 2-methyl-2-propanol + water covering the whole composition range. Furthermore, there are insufficient measurements at high alcohol concentrations over a wide temperaure range. Such data are required for custody transfer of 2-methyl-2-propanol.

The curve filting for excess volume is important to estimate the density of mixtures. Marsh et al. (10) have tried to fit their excess volume data of ethanol + water mixtures to the skewed Redich-Kister function, equation 1, with standard deviations close to experimental error, but they failed. They found that

$$
\begin{equation*}
V_{\mathrm{m}}^{E} /\left(\mathrm{cm}^{3} \mathrm{~mol}^{-1}\right)=x_{\mathrm{a}} x_{\mathrm{w}}\left(\frac{\sum_{i=0}^{n} a_{i}\left(1-2 x_{\mathrm{a}}\right)^{i}}{\left(1+q\left(1-2 x_{\mathrm{a}}\right)\right)}\right) \tag{1}
\end{equation*}
$$

eq 1 does not adequately describe excess volumes of alcohol + water systems due to the steep curvatures in the dilute alcohol region. Davis (11) proposed a four-segmented-composition model which has two water-rich regions, a microheterogeneous region, and an alcohol-rich region. The four-seg-mented-composition model improves the standard deviation in fitting but has discontinuities of its derivatives between segments.
We have measured the excess volumes over the whole composition range at 5 K intervals from 303.15 to 323.15 K and have determined parameters of the switching function whose superiority has been demonstrated in curve fitting excess en-

Table I. Density of Pure 2-Methyl-2-propanol

|  | density, $\mathrm{g} \mathrm{cm}^{-3}$ |  |
| :---: | :---: | :---: |
| $T / \mathrm{K}$ | present work | lit. |
| 303.15 | 0.77521 | $0.775244^{,} 0.77620^{b}$ |
| 308.15 | 0.76997 | $0.77019,^{c} 0.77090^{d}$ |
| 313.15 | 0.76469 | $0.76503^{e}$ |
| 318.15 | 0.75937 |  |
| 323.15 | 0.75401 | $0.75448^{e}$ |
| 328.15 | 0.74861 |  |

${ }^{a}$ Reference 21. ${ }^{b}$ Reference 22. ${ }^{\text {c }}$ Reference 23. ${ }^{d}$ Reference 24. ${ }^{\text {e }}$ Reference 5.
thalpies for ethanol + water by Ott et al. (12).

## Experiment

Three liters of 2-methyl-2-propanol sample (Fluka Chemical Co.) was distilled over freshly ignited calcium oxide (to remove water) in a 2-m distillation column packed with stainiess steel helices (approximately 80 theoretical plates). It was stored over Linde Type 3A molecular sieve which had been activated at $300^{\circ} \mathrm{C}$ under vacuum. All samples were covered by dry nitrogen to exclude atmospheric moisture.

The purities of the samples were determined on a routine basis by gas-liquid chromatography using both a 2-m BP-5 column with a hydrogen flame ionization detector to detect organic impurities and a 2-m Porapak Q column on a Varian 1400 gas chromatography with a thermal conductivity detector to detect water. The purity of 2 -methyl-2-propanol was better than $99.97 \mathrm{~mol} \%$.

The solubility of air in 2-methyl-2-propanol is high, so unless it is thoroughly degassed, the addition of water causes a "salting out" of the air and hence the formation of a bubble, which ruins a dilatometer run. The alcohol and water were thoroughly degassed by either pumping or boiling, or by the use of a multiple freeze-pump-thaw technique.

The temperature was controlled better than $\pm 2 \mathrm{mK}$. All temperatures were measured with a standard platinum resistance thermometer which had been calibrated by the National Bureau of Standards adjusted to IPTS 68.

The densities of pure 2-methyl-2-propanol were measured in a single-arm flash pycnometer having a volume of about 40 $\mathrm{cm}^{3}$ and a $1-\mathrm{mm}$ precision bore tubing marked with a reference line. The accuracy of 2-methyl-2-propanol densities is better than $\pm 1 \times 10^{-5} \mathrm{~g} \mathrm{~cm}^{-3}$. The excess volumes were determined by using a continuous dilution dilatometer described by Stokes et al. (13) and Marsh et al. (10) with an accuracy of better than $\pm 0.001 \mathrm{~cm}^{3} \mathrm{~mol}^{-1}$.

## Results

The densities of pure 2-methyl-2-propanol are given in Table I. Our density values are lower than previous measurements. The freezing point of a purified sample is about 298.87 K . The highest estimated literature freezing point, obtained by extrapolation, is found to be 298.81 K by Simonsen et al. (14). An extrapolated value obtained by Ott et al. (15) is 298.77 K . The higher freezing point and lower densities indicate that our sample probably had a lower water content than pure samples used previously. Values of $V_{\mathrm{m}}^{E} / x_{\mathrm{a}} x_{w}$ are given in Table II and shown in Figures 1 and 2. We estimate that the precision of $V_{m}^{E} / x_{\mathrm{e}} x_{w}$ is better than $\pm 0.2 \%$ over most of the composition range. The primary uncertainty in the measurement arises from the calibration of the 1 -mm-bore capillary.
Values of $V_{m}^{E} / x_{a} x_{w}$ for dilute solutions of 2-methyl-2-propanol are plotted in Figure 2. The partial molar excess volumes of 2-methyl-2-propanol up to $x_{a}=0.05$ shown in Figure 3 are obtained from $\Delta V / \Delta n_{\text {a }}$ for each individual addition where $\Delta V$ is the volume change for the addition of $\Delta n_{a}$ moles of 2 -methyl-2-propanol. The values are plotted against the mean


Figure 1. Excess volumes, expressed as $V_{m}^{E} / x_{a} x_{w}$, for 2-methyl-2propanol $\left(x_{\mathrm{a}}\right)+$ water $\left(x_{w}\right)$ from $x_{\mathrm{a}}=0.1$ to $x_{\mathrm{a}}=1.0$. Experimental results are given for $\Lambda, 303.15 \mathrm{~K}$; $\mathrm{E}, 308.15 \mathrm{~K}$; © $313.15 \mathrm{~K} ; 0$, $318.15 \mathrm{~K} ; \Delta, 323.15 \mathrm{~K}$.


Figure 2. Excess volumes, expressed as $V_{m}^{E} / x_{g} x_{w}$, for 2-methyl-2propanol $\left(x_{\mathrm{a}}\right)+$ water $\left(x_{w}\right)$ from $x_{\mathrm{a}}=0.0$ to $x_{\mathrm{a}}=0.08$. Experimental results are given for $\Delta, 303.15 \mathrm{~K} ; \square, 308.15 \mathrm{~K}$;, 313.15 K ; O , $318.15 \mathrm{~K} ; \Delta, 323.15 \mathrm{~K}$.
value of the mole fraction for the addition.
At $x_{\mathrm{a}}=0.019 \pm 0.001$ the partial molar excess volume is approximately independent of temperature between 303.15 and 323.15 K , having a value of $-9.83 \pm 0.01 \mathrm{~cm}^{3} \mathrm{~mol}^{-1}$. The partial molar excess volumes of 2-methyl-2-propanol at infinite dilution in water, $V_{\mathrm{a}}{ }^{\infty}$, and a partial molar volumes of water at infinite dilution in the alcohol, $V_{w}{ }^{\infty}$, are given in Table III. The temperature dependence of the limiting partial properties are plotted in Figures 4-7.

## Data Evaluation

Ott et al. (12) have investigated the use of an equation containing an exponential switching factor to fit results of the excess enthalples of ethanol + water. Equation 2, which is similar to their equation, was used to fit the excess volumes

Table II. Excess Volumes of 2-Methyl-2-propanol $\left(x_{\mathrm{a}}\right)+$ Water ( $x_{w}$ ) as $V^{E} / x_{\mathrm{a}} x_{w}$ from 303.15 to 323.15 K

| $x_{2}$ | $\begin{aligned} & V^{\mathrm{E}} / x_{\mathrm{a}} x_{\mathrm{w}} / \\ & \mathrm{cm}^{3} \mathrm{~mol}^{-1} \end{aligned}$ | $x_{z}$ | $\begin{aligned} & V^{\mathrm{V}} / x_{\mathrm{a}} x_{\mathrm{w}} / \\ & \mathrm{cm}^{3} \mathrm{~mol}^{-1} \end{aligned}$ | $x_{z}$ | $\begin{aligned} & V^{\mathrm{E}} / x_{\mathrm{a}} x_{\mathrm{w}} / \\ & \mathrm{cm}^{3} \mathrm{~mol}^{-1} \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $T=303.15 \mathrm{~K}$ |  |  |  |  |  |
| 0.00807 | $-7.765$ | 0.04314 | -9.575 | 0.26994 | -4.497 |
| 0.01048 | -8.825 | 0.05750 | -9.193 | 0.29896 | -4.280 |
| 0.01382 | -8.995 | 0.06129 | -8.999 | 0.35511 | -3.932 |
| 0.01720 | -9.158 | 0.06786 | -8.670 | 0.40914 | -3.662 |
| 0.01898 | -9.270 | 0.07152 | -8.495 | 0.46226 | -3.436 |
| 0.02174 | -9.419 | 0.07534 | -8.303 | 0.49446 | -3.300 |
| 0.02621 | -9.618 | 0.08013 | -8.124 | 0.56581 | -3.044 |
| 0.02900 | -9.673 | 0.09698 | -7.426 | 0.60298 | -2.930 |
| 0.03209 | -9.736 | 0.11663 | -6.787 | 0.66682 | -2.688 |
| 0.03506 | -9.796 | 0.15195 | -5.967 | 0.73867 | -2.498 |
| 0.03783 | -9.794 | 0.20107 | -5.108 | 0.81682 | -2.217 |
| 0.04201 | -9.763 | 0.22200 | -4.925 | 0.92963 | -1.830 |
| $T=308.15 \mathrm{~K}$ |  |  |  |  |  |
| 0.00604 | -8.521 | 0.05076 | -9.433 | 0.23366 | -4.886 |
| 0.00784 | -8.685 | 0.06439 | -8.759 | 0.25845 | -4.675 |
| 0.00935 | -8.839 | 0.06887 | -8.509 | 0.29855 | -4.388 |
| 0.01273 | -9.127 | 0.07409 | -8.236 | 0.37051 | -3.996 |
| 0.01622 | -9.346 | 0.08464 | -7.742 | 0.42042 | -3.772 |
| 0.01894 | -9.485 | 0.09407 | -7.379 | 0.47290 | -3.570 |
| 0.02330 | -9.663 | 0.12330 | -6.506 | 0.53848 | -3.349 |
| 0.02674 | -9.739 | 0.14050 | -6.115 | 0.59811 | -3.180 |
| 0.33456 | -9.812 | 0.15663 | -5.819 | 0.65767 | -3.045 |
| 0.04027 | -9.767 | 0.16734 | -5.669 | 0.73968 | -2.863 |
| 0.04445 | -9.658 | 0.18599 | -5.395 | 0.86517 | -2.372 |
| 0.04740 | -9.548 | 0.21408 | -5.079 | 0.96354 | -0.057 |
| $T=313.15 \mathrm{~K}$ |  |  |  |  |  |
| 0.00276 | -8.646 | 0.05321 | -9.239 | 0.45919 | -3.623 |
| 0.00437 | -8.747 | 0.05814 | -8.979 | 0.56392 | -3.295 |
| 0.00649 | -8.874 | 0.06846 | -8.437 | 0.63547 | -3.051 |
| 0.00898 | -9.023 | 0.07553 | -8.098 | 0.71304 | -2.851 |
| 0.01082 | -9.221 | 0.12350 | $-6.507$ | 0.74358 | -2.763 |
| 0.01696 | -9.552 | 0.16555 | -5.642 | 0.77630 | -2.694 |
| 0.02146 | -9.803 | 0.19522 | -5.263 | 0.90114 | -2.216 |
| 0.03555 | -9.909 | 0.21639 | -5.043 | 0.95617 | -2.138 |
| 0.03954 | -9.871 | 0.23850 | -4.832 |  |  |
| 0.43307 | -9.727 | 0.37746 | -3.967 |  |  |
| $T=318.15 \mathrm{~K}$ |  |  |  |  |  |
| 0.05492 | -9.267 | 0.05455 | -9.026 | 0.57164 | -3.383 |
| 0.00731 | -9.374 | 0.06102 | -8.670 | 0.62091 | -3.256 |
| 0.01027 | -9.471 | 0.07595 | -7.976 | 0.64840 | -3.177 |
| 0.01779 | -9.960 | 0.12330 | -6.342 | 0.70402 | -3.059 |
| 0.02168 | -9.977 | 0.15297 | -5.884 | 0.72242 | -2.995 |
| 0.02419 | -10.004 | 0.25276 | -4.756 | 0.78485 | -2.844 |
| 0.03014 | -10.003 | 0.30831 | -4.428 | 0.81236 | -2.681 |
| 0.03383 | -9.925 | 0.34325 | -4.224 | 0.84849 | -2.599 |
| 0.03872 | -9.799 | 0.42389 | -3.884 | 0.88205 | -2.507 |
| 0.04314 | -9.619 | 0.48153 | -3.671 | 0.91803 | -2.433 |
| 0.04754 | -9.403 | 0.50668 | -3.587 | 0.96238 | -2.162 |
| 0.05255 | -9.132 | 0.54555 | -3.462 | 0.97856 | -2.268 |
| $T=323.15 \mathrm{~K}$ |  |  |  |  |  |
| 0.00207 | -9.258 | 0.07209 | -7.820 | 0.45909 | -3.841 |
| 0.00479 | -9.328 | 0.15677 | $-5.820$ | 0.52426 | -3.638 |
| 0.00708 | -9.514 | 0.17893 | -5.515 | 0.56270 | -3.523 |
| 0.01125 | -9.734 | 0.20241 | -5.275 | 0.56270 | -3.523 |
| 0.02111 | -10.159 | 0.22373 | -5.076 | 0.60078 | -3.438 |
| 0.02818 | -10.130 | 0.25990 | -4.791 | 0.63758 | -3.354 |
| 0.03205 | -10.055 | 0.28611 | -4.617 | 0.72019 | -3.245 |
| 0.04106 | -9.692 | 0.30137 | -4.525 | 0.81142 | -2.982 |
| 0.05188 | -9.105 | 0.32603 | -4.397 | 0.84221 | -2.961 |
| 0.05709 | -8.815 | 0.34660 | -4.292 | 0.92753 | -2.691 |
| 0.06076 | -8.612 | 0.37381 | -4.167 |  |  |
| 0.06602 | -8.357 | 0.40289 | -4.047 |  |  |

with a nonlinear curve-fitting program, which minimizes the deviations using a Marquart algorithm (16).

$$
\begin{align*}
& V_{\mathrm{m}}^{E} /\left(\mathrm{cm}^{3} \mathrm{~mol}^{-1}\right)= \\
& x_{\mathrm{a}} x_{\mathrm{w}}\left[e^{-\alpha x_{\mathrm{a}}}\left(\sum_{i=0}^{k} b_{i}\left(1-2 x_{\mathrm{a}}\right)^{\prime}\right)+\left(1-e^{-\alpha x_{\mathrm{a}}}\right) \sum_{l=0}^{m} c_{i}\left(1-2 x_{\mathrm{a}}\right)^{\prime}\right] \tag{2}
\end{align*}
$$

We have chosen $k=1$ and $m=3$. Values of parameters in


Figure 3. Variation of the partial molar excess volume of 2-methyl-2-propanol with concentration for 2-methyl-2-propanol $\left(x_{\mathrm{a}}\right)+$ water $\left(x_{w}\right)$. Experimental results are given for $\mathbf{A}, 303.15 \mathrm{~K} ; 313.15 \mathrm{~K}$; $\Delta, 323.15 \mathrm{~K}$.


Flgure 4. Variation of the partial molar excess volume of water at infinite dilution in 2-methyl-2-propanol, $V_{w}^{E, \infty}$, with temperature.

Table III. Partial Molar Excess Volumes and Partial Molar Volumes for 2-Methyl-2-propanol ( $x_{\text {® }}$ ) + Water ( $x_{\text {w }}$ ) at Infinite Dilution

| $T / \mathrm{K}$ | $V_{\mathrm{w}}^{\mathrm{E}, \infty} /$ <br> $\mathrm{cm}^{3} \mathrm{~mol}^{-1}$ | $V_{\mathrm{w}} \mathrm{m} /$ <br> $\mathrm{cm}^{3} \mathrm{~mol}^{-1}$ | $V_{\mathrm{B}}^{\mathrm{E}, \infty} /$ <br> $\mathrm{cm}^{3} \mathrm{~mol}^{-1}$ | $V_{\mathrm{a}}{ }^{\infty} /$ <br> $\mathrm{cm}^{3} \mathrm{~mol}^{-1}$ |
| :---: | :---: | :---: | :---: | :---: |
| 303.15 | -1.400 | 16.694 | -7.09 | 88.522 |
| 308.15 | -1.601 | 16.523 | -7.70 | 88.555 |
| 313.15 | -1.832 | 16.326 | -8.27 | 88.652 |
| 318.15 | -2.000 | 16.193 | -8.72 | 88.876 |
| 323.15 | -2.140 | 16.094 | -9.11 | 89.207 |

the switching function are listed in Table IV.
In eq 2, the exponential serves as a switching function to change the coefficients in the Redlich-Kister equation from a set which fits the results at low alcohol mole fraction to a set which is valid over the remainder of the composition range. The smaller standard deviations given in Table IV as compared to

Table IV. Parameters of the Switching Function for 2-Methyl-2-propanol $\left(x_{a}\right)+$ Water ( $x_{w}$ )

| $T / \mathrm{K}$ | $\alpha$ | $b_{0}$ | $b_{1}$ | $c_{0}$ | $c_{1}$ | $c_{2}$ | $c_{3}$ | $\sigma / \mathrm{cm}^{3} \mathrm{~mol}^{-1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 303.15 | 29.816 | -134.64 | 128.15 | -3.276 | -1.900 | -1.032 | -1.137 | 0.0018 |
| 308.15 | 32.417 | -131.14 | 124.29 | -3.476 | -1.579 | -1.154 | -1.421 | 0.0019 |
| 318.15 | 29.805 | -107.19 | 98.51 | -3.605 | -1.618 | -0.967 | -0.882 | 0.0017 |
| 323.15 | 31.723 | -107.44 | 98.34 | -3.712 | -1.447 | -1.080 | -1.046 | 0.0014 |

Table V. Parameters of the Skewed Redlich-Kister Function for 2-Methyl-2-propanol ( $\boldsymbol{x}_{\mathrm{a}}$ ) + Water ( $\boldsymbol{x}_{\mathbf{w}}$ )

| $T / \mathrm{K}$ | $a_{0}$ | $a_{1}$ | $a_{2}$ | $a_{3}$ | $a_{4}$ | $a_{5}$ | $q$ | $\sigma / \mathrm{cm}^{3} \mathrm{~mol}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 303.15 | -3.293 | 0.2857 | 0.6894 | -0.9320 | -0.8155 | -0.4128 | -0.64 | 0.0122 |
| 308.15 | -3.481 | 0.4654 | 0.0165 | 0.1417 | 0.155 | -1.9730 | -0.61 |  |
| 313.15 | -3.482 | 0.2153 | 0.2220 | 0.0651 | -0.6157 | -1.8838 | -0.58 | 0.0097 |
| 318.15 | -3.614 | 0.1660 | 0.1881 | 0.5073 | -0.8550 | -2.1557 | -0.52 | 0.0088 |
| 323.15 | -3.721 | 0.1982 | -0.1247 | 1.0247 | -0.5647 | -2.9571 | -0.49 | 0.0075 |
|  |  |  |  |  |  |  |  |  |



Figure 5. Variation of the partial molar volume of water at infinite dilution in 2-methyl-2-propanol, $V_{a}^{\infty}$, with temperature.
those in Table V show the superiorlty of eq 2 over eq 1 in filting $V_{m}^{E}$ at $303.15,308.15,313.15,318.15$, and 323.15 K for the 2-methyl-2-propanol + water system.

## Discussion

Excess volumes calculated from the density results of Kenttamaa et al. (5) at 313.15 and 323.15 K are about 0.009 $\mathrm{cm}^{3} \mathrm{~mol}^{-1}$ less negative than our data in the water-rich region. However, above $x_{\mathrm{a}}=0.05$ the agreement with our data is generally within $0.001 \mathrm{~cm}^{3} \mathrm{~mol}^{-1}$. Their value for the limiting partial molar excess volumes of 2-methyl-2-propanol are about $2.3 \mathrm{~cm}^{3} \mathrm{~mol}^{-1}$ more positive than our results. These differences can be ascribed to impurties in 2-methyl-2-propanol and their extrapolation method. Their values for densities of 2 -methyl-2-propanol at 313.15 and 323.15 K are 0.76499 and 0.75448 $\mathrm{g} \mathrm{cm}{ }^{-3}$, respectively, which are $0.05 \%$ greater than the present results of 0.76469 and $0.75401 \mathrm{~g} \mathrm{~cm}^{-3}$. The higher densities indicate that the alcohol used for their measurements might contain more than $0.03 \mathrm{~mol} \%$ water.

Values of excess volumes obtained from the apparent molal volumes of Visser et al. (17) at 313.15 K agree with our results within the combined experimental error. Their value for the partial molar volume of $88.63 \mathrm{~cm}^{3} \mathrm{~mol}^{-1}$ for 2-methyl-2propanol at infinite dilution in water at 313.15 K is slightly lower than our value of $88.65 \mathrm{~cm}^{3} \mathrm{~mol}^{-1}$. This difference between the estimates may be ascribed to well-known problems involved in the extrapolation of the experimental data to zero concentration. The strong concentration dependence in the water-rich region and the scattering of values of apparent molal volumes


Figure 6. Variation of the partial molar excess volume of 2-methyl-2-propanol at infinite dilution in water, $V_{a}^{E, \infty}$, with temperature.


Figure 7. Variation of the partial molar volume of 2-methyl-2-propanol at infinite dilution in water, $V_{a}{ }^{\infty}$, with temperature.
of $x_{\mathrm{a}}$ approaching zero complicate the extrapolation.
Franks and Watson (18) have related the change in the temperature of maximum density, $\Delta \theta$, to the variation of the
excess volume with temperature $\left(\partial V_{\mathrm{m}}^{E} / \partial T\right)_{P}$ by

$$
\begin{align*}
\Delta \theta=\Delta \theta_{\mathrm{i}}+ & \Delta \theta_{\mathrm{s}}= \\
& \frac{x_{\mathrm{a}} \alpha_{\mathrm{a}} V_{\mathrm{a}}^{0}(273.15 \mathrm{~K})}{2 \alpha_{\mathrm{w}} V_{\mathrm{w}}^{0}(277.13 \mathrm{~K})}-\frac{\left(\partial V_{\mathrm{m}}^{E} / \partial T\right)_{\mathrm{P}}}{2 \alpha_{\mathrm{w}} x_{\mathrm{w}} V_{\mathrm{w}}(277.13 \mathrm{~K})} \tag{3}
\end{align*}
$$

where $V_{\mathrm{g}}{ }^{\circ}(273.15 \mathrm{~K})$ is the extrapolated molar volume of the alcohol at $273.15 \mathrm{~K}, V_{w}{ }^{0}(277.15 \mathrm{~K})$ is the molar volume of pure water at the temperature of maximum density, and $\alpha_{\mathrm{a}}$ and $\alpha_{\mathrm{w}}$ are coefficients of thermal expansion of alcohol and water. $\Delta \theta_{\mathrm{i}}$ and $\Delta \theta_{\mathrm{s}}$ are temperatures of maximum density due to the ideal mixing and structural change, respectively. The maximum of $\Delta \theta_{\mathrm{s}}$ occurs at $x_{\mathrm{a}}=x_{\mathrm{a}}{ }^{*}$ as pointed by Armitage et al. (19).

$$
\begin{equation*}
\left(\frac{\partial \Delta \theta_{\mathrm{s}}}{\partial x_{\mathrm{a}}}\right)_{x_{\mathrm{a}}=x_{\mathrm{a}}}=-\frac{\partial\left(\partial\left(V_{\mathrm{m}}^{E} / x_{\mathrm{w}}\right) / \partial x_{\mathrm{a}}\right)_{x_{\mathrm{a}}=x_{\mathrm{a}}}}{\partial T}=0 \tag{4}
\end{equation*}
$$

hence

$$
\begin{equation*}
\left(\partial V_{\mathrm{a}}^{\varepsilon} / \partial T\right)_{x_{\mathrm{a}}=x_{\mathrm{a}}}=0 \tag{5}
\end{equation*}
$$

Figure 3 shows that the partial molar excess volume of 2-methyl-2-propanol at low values of $x_{\mathrm{a}}, V_{\mathrm{a}}^{E}$, is strongly temper-ature-dependent, becoming more negative as the temperature increases. At $x_{\mathrm{a}}{ }^{*}=0.019$, the partial molar excess volume of 2-methyl-2-propanol is independent of temperature, having a value of $-9.83 \mathrm{~cm}^{3} \mathrm{~mol}^{-1}$. The excess volume is independent of temperature at $x_{\mathrm{a}}{ }^{* *}=0.039$ as shown in Figure 2 with $-0.0376 \mathrm{~cm}^{3} \mathrm{~mol}^{-1}$. The mole fraction of alcohol where $\left(\partial V_{\mathrm{E}}^{E} / \partial T\right)=0$ is half the mole fraction of alcohol at which $\left(\partial V_{m}^{e} / \partial T\right)=0$. This would indicate that $\Delta \theta_{\mathrm{s}}$ has a quadratic relationship to $x_{\mathrm{a}}$. Above $x_{\mathrm{a}}=0.039$, the partial molar volume and excess volume increase with increase in temperature.

The pairwise interaction of alkyl groups of alcohol at infinite dilution is observed from the apparent molar volume model suggested by Franks (20). The apparent molar volume at infinite dilution of alcohol, $V_{\text {app }}$, is related to the pair ( $v_{x x}$ ) and triple $\left(v_{\mathrm{xxx}}\right)$ interaction coefficients between nonpolar groups in the solute molecule.

$$
\begin{equation*}
V_{\mathrm{app}}-V_{\mathrm{a}}^{\infty}=\left(V_{\mathrm{a}}^{0}+V_{\mathrm{a}}^{E}\right)-V_{\mathrm{a}}^{\infty}=v_{\mathrm{xx}} x_{\mathrm{a}}+v_{\mathrm{xxx}} x_{\mathrm{a}}^{2}+\ldots \tag{6}
\end{equation*}
$$

$V_{a}{ }^{0}$ is the pure molar volume of 2-methyl-2-propanol. Negative slopes of $V_{\mathrm{a}}^{E}$ at infinite dilution indicate that pairwise interactions of $v_{x x}$ contribute to decreasing the excess and partial excess volumes for aqueous alcohol solutions. The pairwise interaction decreases in magnitude with rising temperature and approaches zero at 323.15 K . The decrease of partial excess volume of alcohol with increasing molar concentration of alcohol in the dilute region is ascribed to the solute-solute interaction.

Nakanishi et al. (25) and Tanaka et al. (26) have recently published molecular dynamics simulations on an infinite dilute and a $3 \mathrm{~mol} \%$ 2-methyl-2-propanol solution in water. They observe a large negative molar excess volume of the alcohol. From a study of the partial radial distribution functions of each of the species they conclude that the water structure is promoted and the alcohol molecule occupies the cavity of the water structure. This result in a very large negative excess volume which is partly compensated by a small volume increase of water around 2-methyl-2-propanol due to hydrophobic hydration effect. In addition to hydrophobic hydration at finite concentrations, the hydrophobic interaction leads to the overlapping of the hydration sphere and thus a further decrease in the excess volume at the dilute alcohol region. They could conclude nothing about more concentrated solutions.

Registry No. 2-Methyl-2-propanol, 75-65-0.

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